

ARTICLE OPEN



Unraveling energy and charge transfer in type-II van der Waals heterostructures

Junyi Liu¹, Zi Li², Xu Zhang¹ and Gang Lu¹✉

Recent experiments observed significant energy transfer in type-II van der Waals (vdW) heterostructures, such as $WS_2/MoSe_2$, which is surprising due to their staggered band alignment and weak spectral overlap. In this work, we carry out first-principles calculations to shed light on energy and charge transfer in $WS_2/MoSe_2$ heterostructure. Incorporating excitonic effect in nonadiabatic electronic dynamics, our first-principles calculations uncover a two-step process in competing energy and charge transfer, unravel their relative efficiencies and explore the means to control their competition. While both Dexter and Förster mechanisms can be responsible for energy transfer, they are shown to operate at different conditions. The excitonic effect is revealed to drive ultrafast energy and charge transfer in type-II $WS_2/MoSe_2$ heterostructure. Our work provides a comprehensive picture of exciton dynamics in vdW heterostructures and paves the way for rational design of novel vdW heterostructures for optoelectronic and photovoltaic applications.

npj Computational Materials (2021)7:191; <https://doi.org/10.1038/s41524-021-00663-w>

INTRODUCTION

Van der Waals (vdW) heterostructures composed of vertically stacked two-dimensional (2D) layers are attracting enormous attention^{1–3}, as they provide a fascinating playground to explore both fundamental physics^{4–6} and novel applications^{7,8}. Among 2D materials, transition metal dichalcogenides (TMDs) are of particular interest owing to their strong light–matter interactions^{9,10} and strong spin–orbit coupling (SOC)^{11,12}. Moreover, due to quantum confinement and reduced dielectric screening, TMD monolayers and their heterostructures feature prominent excitonic effect with large exciton binding energy in the range of 0.3–1.1 eV^{13–18}. Stable and diverse exciton species, including bright intralayer excitons, momentum-forbidden indirect interlayer excitons, hybridized excitons, and spin-forbidden dark excitons have been observed in TMD heterostructures^{19–22}. The accessibility to valley degrees of freedom coupled with rich exciton physics render TMD heterostructures an ideal platform for exploiting charge and exciton dynamics at nanoscales.

In vdW heterostructures, both charge and energy transfer can take place and compete with each other^{3,23}. While charge transfer is crucial in applications such as photovoltaics²⁴, photocatalysis²⁵, and photodetectors²⁶, energy transfer is essential to light-emitting diodes²⁷, sensors²⁸, and lasers²⁹, etc. As charge and energy transfer compete with each other, one of them has to be promoted while the other suppressed for a given application. While charge transfer is believed to be a dominant process in type-II heterojunctions^{30–32}, energy transfer is generally expected to take place in type-I heterojunctions^{33–36}. However, recent experiments have observed significant energy transfer in type-II TMD heterojunctions^{37–39}. Kozawa et al.³⁷ were among the first to report energy transfer in type-II $MoSe_2/WS_2$ heterostructure on the basis of enhanced photoluminescence (PL) in $MoSe_2$ layer under an excitation resonant with the optical band gap of WS_2 layer. The energy transfer from WS_2 to $MoSe_2$ is efficient and ultrafast (<1 ps) at low temperatures (5–200 K)³⁷. Moreover, the energy transfer can be enhanced by separating $MoSe_2$ and WS_2 with insulating

h-BN layers³⁷. Energy transfer was also observed in type-II heterostructures of MoS_2/WS_2 separated by insulating layers of h-BN^{38,39}. Although the experimental evidence of energy transfer in type-II heterostructures is clear, the underlying mechanism remains elusive. Based on temperature dependence of energy transfer rates, Kozawa et al.³⁷ proposed that the energy transfer follows Förster mechanism⁴⁰, which involves excitons in WS_2 exciting higher-order excitons in $MoSe_2$ via a direct dipole–dipole interaction. However, low-energy excitons in TMD heterostructures tend to be non-emissive dark excitons whose dipole–dipole interactions are normally too weak to yield efficient Förster energy transfer. Based on this argument, Dexter mechanism⁴¹, consisted of simultaneous transfer of electron and hole, was proposed to be responsible for ultrafast energy transfer in type-I $WSe_2/MoTe_2$ heterostructure³⁶. Compounding to the confusion, the origin of efficient energy transfer in $MoSe_2/WS_2$ heterostructure is poorly understood; it is not clear what is the driving force of simultaneous electron and hole transfer in the staggered type-II band alignment. This is particularly puzzling given weak temperature dependences of energy and charge transfer rates³⁷, which rules out thermal fluctuations as the driving force. Therefore, it is of fundamental importance to elucidate the mechanism and unravel the competition of energy and charge transfer in type-II vdW heterostructures. It is also of timely, practical interest to explore exciton dynamics and seek control of energy and charge transfer in vdW heterostructures. However, despite scientific importance and practical interest, little work has been devoted to the competition of energy and charge transfer in vdW heterostructures, especially from a theoretical perspective. To the best of our knowledge, no energy transfer in TMD heterostructures has been studied by first principles. Thus, in this work we aim to fill the knowledge gap by providing a first-principles picture of energy and charge transfer in $MoSe_2/WS_2$ heterostructure.

The main challenge in first-principles studies is that excitonic effect must be included because the strong Coulomb interactions

¹Department of Physics and Astronomy, California State University, Northridge, CA 91330-8268, USA. ²Institute of Applied Physics and Computational Mathematics, P.O. Box 8009, Beijing 100088, China. ✉email: ganglu@csun.edu

between electrons and holes have profound effects on the dynamics of energy and charge transfer in TMD heterostructures^{3,42}. The conventional first-principles approach to capture the excitonic effect is GW-Bethe-Salpeter equation (GW-BSE) method^{43–45} based on many-body perturbation theory. However, it is prohibitively expensive to perform dynamics simulations with the GW-BSE method. To overcome this challenge, we employ a recently developed first-principles method based on the linear-response time-dependent density functional theory (LR-TDDFT)^{46,47}, which is computationally much more expeditious than the GW-BSE method. To unravel the competing dynamics of energy and charge transfer, we combine the nonadiabatic molecular dynamics (NAMD) with LR-TDDFT in this work. Specifically, we first perform ab initio Born-Oppenheimer molecular dynamics (BOMD) simulations for the MoSe₂/WS₂ heterostructure. At each BOMD timestep, the excitation energies and many-body wavefunctions are determined with LR-TDDFT calculations using optimally tuned, screened, and range-separated hybrid (OT-SRSH) exchange-correlation (XC) functionals^{48–51} implemented in conjunction with plane waves and pseudopotentials^{52–60}. The time-dependent excitonic wavefunctions are then expanded in terms of these many-body wavefunctions⁶¹, with expansion coefficients computed from the fewest-switches-surface-hopping (FSSH) NAMD simulations^{62–64}. Each coefficient represents the probability amplitude that a given exciton makes a transition from an initial state to a specified excitonic state. The phonon-assisted excitonic transitions are captured by the nonadiabatic coupling matrix elements which depend on the time-dependent wavefunctions and excitation energies of the system⁶¹. In sharp contrast to local and semi-local XC functionals, the OT-SRSH functionals can reproduce the correct long-range electron–electron and electron–hole interactions in solids with appropriate screening⁵¹, which enables the LR-TDDFT to capture the excitonic effect in extended systems. The details of the LR-TDDFT and NAMD methods can be found in Supplementary Methods. In particular, comparisons with available experimental and GW-BSE values of the band gaps and exciton binding energies are included in Supplementary Table 1. The combined LR-TDDFT and NAMD framework has been used to study exciton dynamics in WS₂/MoSe₂ heterostructures⁴², ZnO/polymer heterostructures⁶⁵, conjugated polymers⁶¹, and small molecules^{66,67} for photovoltaic applications.

RESULTS

Static properties of MoSe₂/WS₂ heterobilayer

The single-particle band structure calculated using the conventional hybrid XC functional (HSE06)⁶⁸ combined with SOC for the hexagonal unit cell is displayed in Fig. 1b. For the equilibrium structure ($d = 3.3$ Å), our calculations confirm the type-II band alignment in MoSe₂/WS₂ heterostructure³⁷, where the conduction band minimum (CBM) and the valence band maximum (VBM) reside on WS₂ (in deep red) and MoSe₂ (in deep blue) layer, respectively. Based on a band unfolding analysis, we can identify the original *K*-valley states of the constituent monolayers in the band structure of the heterostructure, and label them by black circles for *K*@WS₂ and red triangles for *K*@MoSe₂ in Fig. 1b. The conduction band energy of *K*@MoSe₂ is only 42 meV higher than that of *K*@WS₂, which suggests a small band offset for the electrons at *K*-valley and agrees with the previous results^{69,70}. There is a hybridized valence band (~100 meV below the VBM), highlighted in the dashed box with a light blue color, which arises from the interlayer coupling. As the interlayer distance is increased to $d = 8.3$ Å, this hybridized band drops in energy and disappears from the energy window (Supplementary Fig. 3), which has consequences as discussed below. Note that the single-particle band structure shown here only serves the purpose to define the relevant excitonic transitions. The energies of these excitons are

actually determined based on LR-TDDFT with the OT-SRSH functional.

We next perform the LR-TDDFT calculations with the OT-SRSH functional to examine the excitonic properties at zero temperature. In the TDDFT and subsequent BOMD (and NAMD) calculations, the larger orthogonal supercell (the red dashed box in Fig. 1a) is used instead. In this work, we focus on singlet excitons as they have lower energies and are the subject of the experimental studies which we will compare to. Specifically, five low-energy singlet excitons are considered, and their charge densities (see Supplementary information for the definition) are shown in Fig. 1b: (i) \tilde{S}_1 is an interlayer exciton comprised primarily of an electron from CBM@WS₂ and a hole from VBM@MoSe₂; \tilde{S}_1 is the lowest-energy exciton in the heterostructure (1.64 eV); (ii) S_{Mo} is an intralayer exciton with both its electron and hole from *K*@MoSe₂, corresponding to the A exciton of MoSe₂ monolayer. S_{Mo} is the second lowest-energy exciton (1.65 eV) and responsible for energy transfer in the heterostructure; (iii–iv) \tilde{S}_2 and \tilde{S}_3 are two interlayer excitons whose holes are spread over both layers while electrons are localized at WS₂ and MoSe₂ monolayer, respectively. The energy of \tilde{S}_2 and \tilde{S}_3 is 1.75 and 1.80 eV, respectively; and (v) S_0 is an intralayer exciton with 100% of its electron and 80% of its hole localized at WS₂. S_0 (2.01 eV) corresponds to the A exciton in WS₂ monolayer and also the initial excitation (or pump) in the pump-probe experiments³⁷. To distinguish the intra- and inter-layer excitons, we label the interlayer excitons with a tilde (~) on the top. Owing to the atomic-scale interlayer distance (~3 Å), even the intralayer excitons have small amounts of electrons or holes spilled across the layers, dictated by the uncertainty principle. The calculated oscillator strength for the interlayer excitons, \tilde{S}_1 , \tilde{S}_2 , \tilde{S}_3 is 0.005, 0.028, 0.03, respectively, and these excitons are considered as dark excitons. In contrast, the oscillator strength for the intralayer excitons S_{Mo} and S_0 is 0.74 and 0.15, respectively, and thus they are bright excitons with stronger absorption and radiative emission.

Exciton dynamics from many-body NAMD simulations

In the following, we perform NAMD simulations at 300 K to examine the decay dynamics of the initial exciton (S_0) and as well as the formation dynamics of the interlayer excitons (\tilde{S}_1 , \tilde{S}_2 , \tilde{S}_3) and the intralayer exciton S_{Mo} . The transitions from S_0 to \tilde{S}_1 , \tilde{S}_2 , \tilde{S}_3 contribute to charge transfer while the transition from S_0 to S_{Mo} is considered as energy transfer. As shown in Fig. 2a, there is an ultrafast decay of the initial exciton S_0 , whose population decreases drastically in ~11 fs. During this time, the average energy of the excitons is only slightly reduced as shown Fig. 2c, suggesting ultrafast transfer of S_0 to intermediate “hot” excitons. These hot excitons subsequently cool down and relax to low-energy excitons at a longer timescale. In 500 fs, about 15% of the initial S_0 excitons decay into the intralayer exciton (S_{Mo}) via energy transfer, and ~30% of the initial excitons decay into the interlayer excitons (\tilde{S}_1 , \tilde{S}_2 , \tilde{S}_3) via charge transfer. The detailed dynamics for the low-energy excitons are shown in the Fig. 2b. The remaining initial excitons transfer to intermediate excitons with approximate 32% of interlayer character and 18% of intralayer character. The dominant exciton species contributing to charge transfer is the interlayer exciton \tilde{S}_1 while the dominant species for energy transfer is the intralayer exciton S_{Mo} , thanks to their low energies. The bright intralayer exciton S_{Mo} would eventually radiatively recombine to yield the enhanced PL intensity observed in the experiment³⁷. The two-step dynamics, i.e., the ultrafast decay to intermediate hot excitons followed by a slower relaxation to low-energy excitons, is also observed at 50 K as shown in Fig. 2d. This two-step process appears general in TMD vdW heterostructures^{36,42,71}. From Fig. 2d, two characteristic timescales (~48 and ~200 fs) can be identified, with the former (~48 fs) corresponding to the ultrafast decay of S_0 and the latter (~200 fs) being where S_0

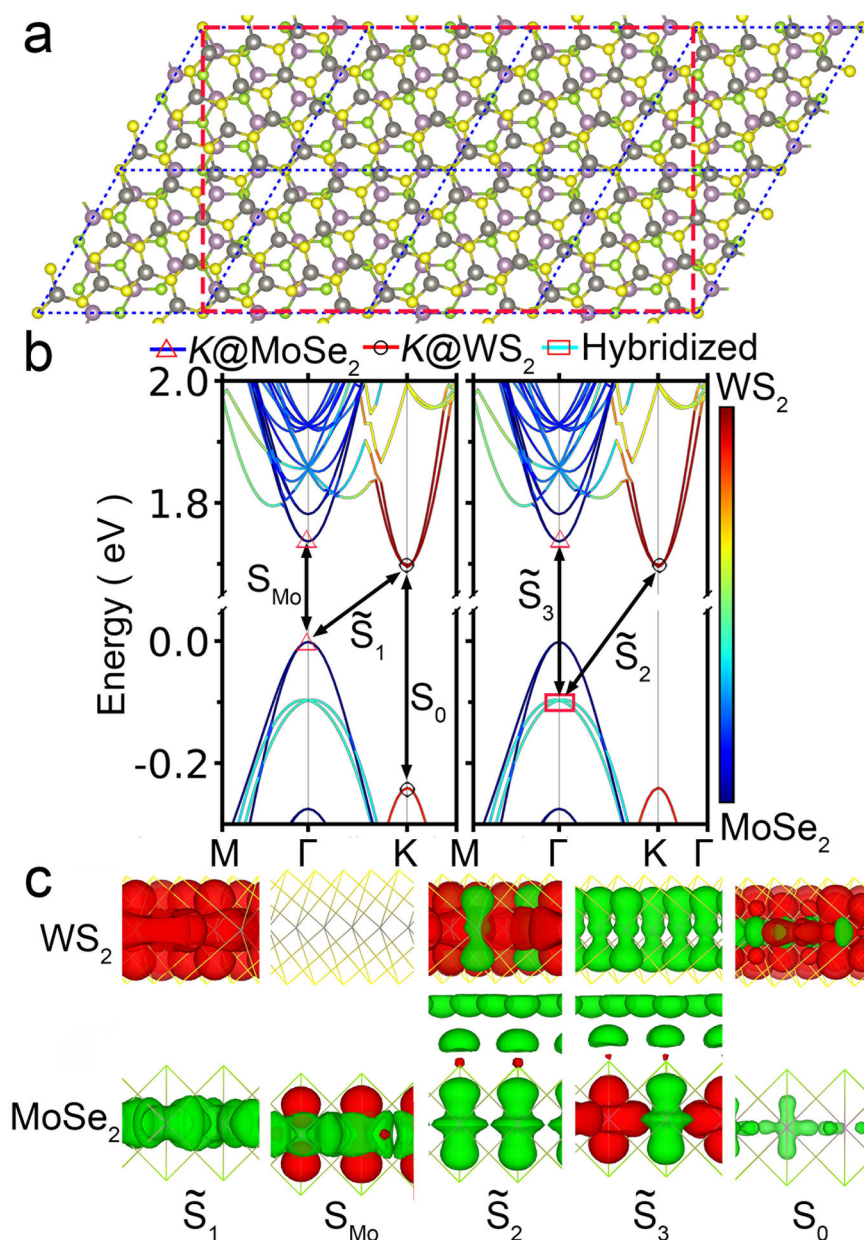


Fig. 1 The atomic structure, band structure, and exciton charge densities of MoSe₂/WS₂ heterobilayer. **a** The top view of the hexagonal unit cell (blue dashed box) and the orthogonal supercell (red dashed box) for the MoSe₂/WS₂ heterobilayer, where purple, green, gray, and yellow spheres representing Mo, Se, W, and S atoms, respectively. **b** The single-particle band structure of the MoSe₂/WS₂ heterobilayer. The same band structure is duplicated in both panels for a clear view of the five excitations. The projection of each band onto WS₂ (deep red) and MoSe₂ (deep blue) layer is color-coded with the sliding bar (with hybridized bands represented by colors between the deep red and deep blue). **c** The side view of the charge densities (see Supplementary Methods for the definition) of the five excitons with the red and green color representing the quasi-electron and quasi-hole, respectively. The iso-surface value is set at $1 \times 10^{-4} \text{ \AA}^{-3}$.

decay curve intercepts the energy/charge transfer curves. Both match well to the experimentally observed upper (15–45 fs) and lower (~200 fs) bounds for the timescale of energy/charge transfer at low temperatures (5–200 K)³⁷. Also consistent with the experiment³⁷, the charge and energy transfer rates show a weak dependence on temperature (50 K vs. 300 K). Interestingly, the energy decay is much greater at 300 K than at 50 K as shown in Fig. 2d, suggesting much stronger electron–phonon coupling at 300 K, leading to a faster decay time (11 fs) at 300 K. We have also performed NAMD calculations at 50 K with the MoSe₂ A exciton (S_{Mo}) as the initial state. The results are shown in Supplementary Fig. 4; similar sub-50 fs ultrafast charge transfer (43 fs) from S_{Mo} to \tilde{S}_1 is observed.

To shed light on competing energy and charge transfer, we examine the energy variation of the excitons (\tilde{S}_1 , S_{Mo} , S_M , and S_0) at 50 K as shown in Fig. 3a. S_M represent “hot” intermediate states whose energy range is also highlighted in Fig. 3b. Due to thermal fluctuations, the degeneracy of the excitonic states at 0 K is broken, and as a result, four groups of energetic curves are formed, each represented by a different color. The energy of the initial exciton S_0 overlaps strongly with that of S_M , yielding ultrafast decay (~50 fs) from S_0 to S_M via adiabatic transitions. The intermediate hot excitons (S_M) subsequently relax to the low-energy excitons (e.g., \tilde{S}_1 and S_{Mo}) via nonadiabatic processes. The much longer relaxation process is due to the substantial energy difference between the intermediate excitons (S_M) and the

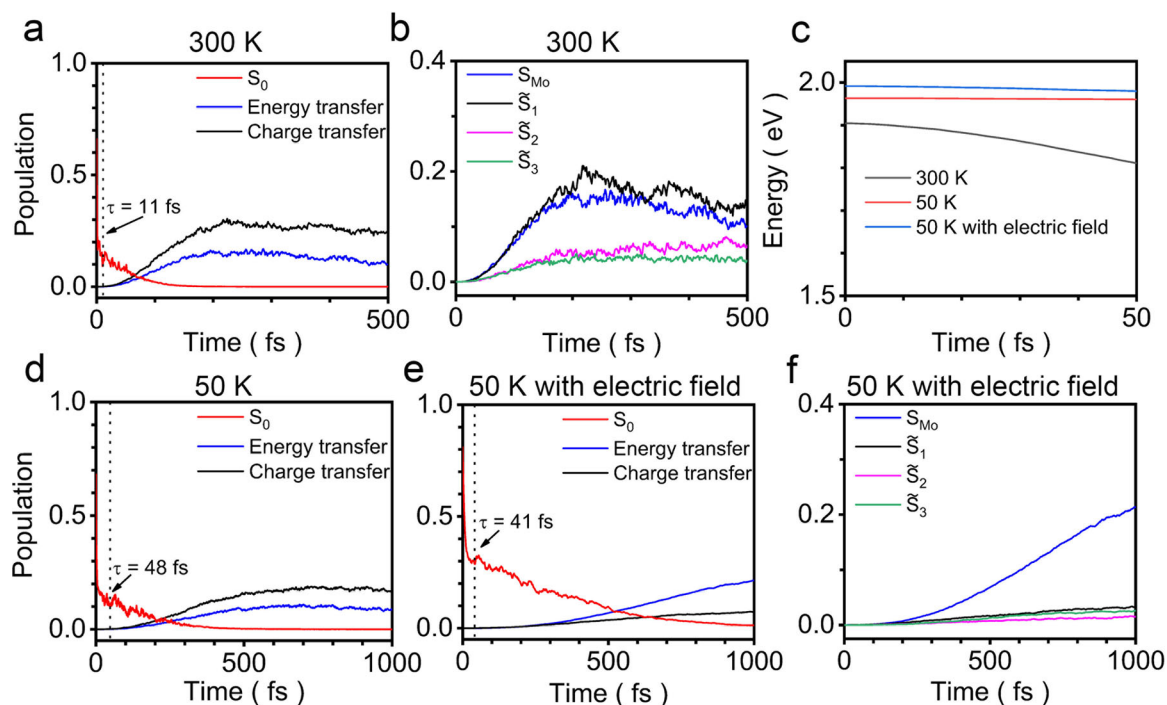


Fig. 2 Results from many-body NAMD simulations. Time-dependent population of the initial exciton (S_0) and other low-energy excitons (S_{Mo} , \tilde{S}_1 , \tilde{S}_2 , \tilde{S}_3) at 300 K (a) and 50 K in the absence (d) and presence (e) of an applied electric field. The individual contribution from each exciton is shown in (b) in the absence of the electric field and (f) in the presence of the electric field. The average energy of the excitons during the NAMD simulations in the first 50 fs is shown in (c).

low-energy excitons (\tilde{S}_1 and S_{Mo}). On the other hand, the energy overlap between the intralayer exciton S_{Mo} and the interlayer exciton \tilde{S}_1 signifies the competing energy and charge transfer in $MoSe_2/WS_2$. This is in contrast to other type-II TMD heterostructures (e.g., MoS_2/WS_2 ⁴²) with larger band offsets. Much less energy transfer was observed in MoS_2/WS_2 ⁴² due to a larger energy gap between the corresponding intralayer and interlayer excitons.

Since the average energy of \tilde{S}_1 is lower than S_{Mo} , charge transfer is expected to be more efficient than energy transfer as observed in Fig. 2. On the other hand, being the lowest-energy exciton, \tilde{S}_1 does not have broad energy overlap with other excitons, thus phonon-assisted transitions are limited for \tilde{S}_1 , whose energy exhibits a stronger harmonic (or quasi-periodic) variation as compared to other excitons. In Fig. 4, we present the Fourier transform of time-dependent energy variation of S_0 , \tilde{S}_1 , and S_{Mo} . It is found that S_{Mo} is driven primarily by phonons around 200 cm^{-1} , corresponding to out-of-plane A_{1g} and in-plane E_{1g} optical modes in $MoSe_2$ layer. In contrast, \tilde{S}_1 is strongly coupled to phonons around 400 cm^{-1} , corresponding to A_{1g} optical mode in WS_2 layer. In addition to A_{1g} mode in WS_2 , S_0 also couples to low-frequency acoustic modes. Selective phonon coupling of \tilde{S}_1 and S_{Mo} suggests that the competition of energy and charge transfer may be tuned by exciting different phonons. Finally, the smaller energy variation of S_{Mo} (compared to \tilde{S}_1 and S_0) shown in Fig. 3a can be attributed to the lower energy phonons that it couples to.

To elucidate the energy and charge transfer mechanism, we examine the charge density evolution of the initial exciton S_0 during the first 50 fs of the NAMD simulation at 50 K. Specifically, one of the most probable NAMD trajectories is identified and along which the charge density of S_0 is calculated, shown in Fig. 3c. A direct and ultrafast charge transfer—with both electron and hole—between the two layers is observed. Specifically, a simultaneously transfer of the electron and the hole takes place at 30 fs, indicating that the Dexter mechanism is at play. Moreover, the excitons (S_M) involved in the energy transfer are those with intermediate energies between 1.95 and 2.01 eV. As shown in

Supplementary Fig. 5, the electron and the hole can find themselves in both layers with minor energy differences, suggesting facile energy transfer via the Dexter mechanism. The intermediate excitons include both intralayer excitons on $MoSe_2$ and interlayer excitons. Note that they are not free electron–hole pairs because their excitation energies are less than the quasiparticle gap of 2.18 eV (Supplementary Table 1), thus their binding energies are greater than 0.17 eV. We have also calculated the oscillator strengths of the intermediate excitons, shown in Fig. 3b. They are found to have much smaller oscillator strengths compared to the bright exciton S_{Mo} (dashed oval). This suggests that the direct dipole–dipole interactions between them may be too weak to yield ultrafast and efficient energy transfer. Thus, Förster energy transfer is not believed to play an important role in $MoSe_2/WS_2$ bilayer. The fact that Dexter mechanism is primarily responsible for energy transfer in $MoSe_2/WS_2$ should not be surprising because ultrafast charge transfer (<150 fs) of either electron or hole has been routinely observed in TMD heterostructures with type-II band alignment^{30,32,71–73}, thanks to their small interlayer distances (<1 nm).

Single-particle NAMD simulations

To uncover the excitonic effect on energy transfer in $MoSe_2/WS_2$ bilayer, we perform a contrasting NAMD simulation in the absence of many-body excitonic interaction. Specifically, the ground state DFT—as opposed to the excited state LR-TDDFT—calculations are carried out at each BOMD timestep. The time-dependent single-particle Kohn–Sham (KS) orbitals and energies, as opposed to the many-body wavefunctions and exciton energies, are obtained from these ground state DFT calculations. The time-dependent single-particle wavefunctions of “excited” electrons or holes are then expanded in terms of these KS orbitals and the expansion coefficients represent the probability amplitude of the “excited” electron or hole occupying one of the KS orbitals, which can be determined from FSSH-NAMD simulations. The excited electron

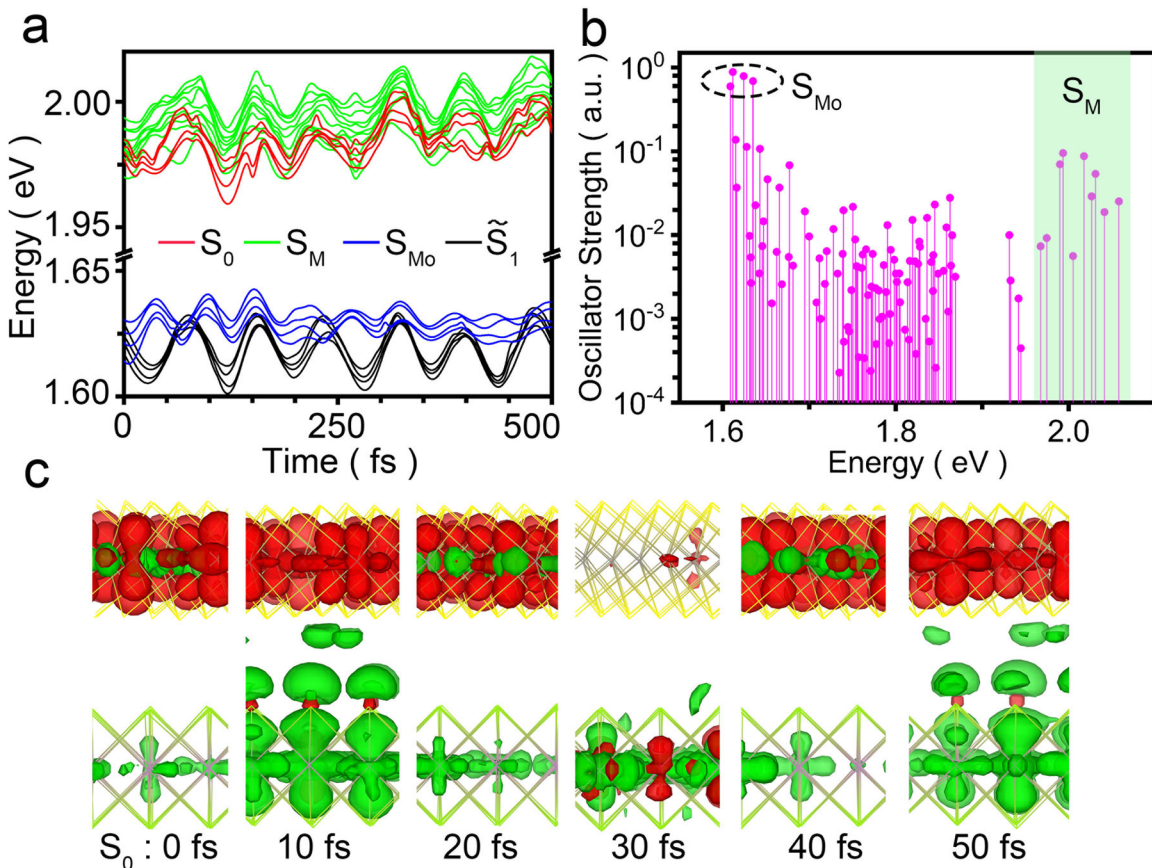


Fig. 3 Exciton energy fluctuation, oscillator strength, and charge density. **a** The time evolution of exciton energies at 50 K for the four exciton states. **b** The oscillator strength on a logarithmic scale for selected excitons, with S_{Mo} (S_M) at the lower (higher) energy end. **c** The snapshots of charge density for S_0 during NAMD simulations (in 50 fs) with the red and green color denoting the quasi-electron and quasi-hole, respectively. The iso-surface value is set at $1 \times 10^{-4} \text{ \AA}^{-3}$.

initially occupies the lowest K -valley-conduction band of WS_2 , while the hole occupies the highest K -valley valence band of WS_2 , corresponding to the resonant excitation (A exciton) of WS_2 in the experiment³⁷. The population dynamics of the “excited” hole and electron are displayed in Fig. 5a, b, respectively. It is found that the “excited” hole decays to intermediate valence states in ~ 50 fs and about 20% of the holes are transferred to the K -valley of $MoSe_2$ in 1 ps. However, the “excited” electron in WS_2 cannot transfer to $MoSe_2$, but remains at the K -valley of WS_2 during the entire NAMD simulation time of 1 ps. The forbidden electron transfer is due to the energy gap between the K -valley states of the electron at WS_2 and $MoSe_2$, as shown in Fig. 5c. The thermal fluctuation at 50 K is not sufficient to overcome the energy gap. Therefore, in the absence of the excitonic effect, one would conclude that while charge transfer (via holes) is possible, energy transfer is forbidden in $WS_2/MoSe_2$ at low temperatures; the latter of course is contradictory to the experiment³⁷. These results have several important implications: (1) They demonstrate that the excitonic effect is the origin of energy transfer in type-II TMD heterostructures. The strong electron–hole interaction renders the overlap in energy between the interlayer exciton \tilde{S}_1 and intralayer exciton S_{Mo} , thus promotes efficient energy transfer. In other words, the electron–hole binding provides the driving force for the electron to overcome the energy barrier. The aid from thermal fluctuations is not critical for energy transfer, which explains the weak temperature dependence of energy transfer in $WS_2/MoSe_2$. (2) NAMD simulations based on the single-particle description are not justified in TMD heterostructures even if they may yield seemingly correct numbers. (3) The commonly used energy

alignment diagrams for TMD heterostructures can be misleading because they are based on single-particle energy levels of monolayers. Without considering the excitonic effect, one may draw a wrong conclusion that electron transfer cannot take place in type-II $WS_2/MoSe_2$, thus rule out the Dexter mechanism erroneously³⁷.

Tuning the competition of energy and charge transfer

It is of significant interest to be able to tune the competition of energy and charge transfer in vdW heterostructures. In the following, we explore two means of tuning energy and charge transfer in vdW heterostructures—the application of an electric field and altering interlayer distance. First, we apply a vertical electric field of pointing from WS_2 to $MoSe_2$ and carry out the same LR-TDDFT calculations. The exciton energies at 0 K under the electric field are shown in the last rows of Table 1. Since the intralayer excitons (S_0 and S_{Mo}) have in-plane dipoles, the Stark interaction is negligible, thus their energies are barely changed. The interlayer excitons \tilde{S}_2 and \tilde{S}_3 with delocalized holes in both layers also exhibit minor changes (~ 0.05 eV) in energy under the electric field. In contrast, the interlayer exciton \tilde{S}_1 has a larger vertical dipole moment, hence its energy increases by 0.11 eV under the electric field. We next perform NAMD simulations to examine the energy and charge transfer dynamics under the electric field. As shown in Fig. 2e, the similar two-step dynamics is observed. However, the relaxation process is slowed down considerably in the presence of the electric field because the energy gaps between S_0 and the intermediate excitons are increased by the electric field. More importantly, $\sim 20\%$ of the

initial excitons decay into the intralayer exciton S_{Mo} via energy transfer, doubling the energy transfer efficiency in the absence of the electric field. As shown in Fig. 2f, the population of the intralayer exciton S_{Mo} increases substantially at the expense of the interlayer exciton \tilde{S}_1 . Thus, the electric gating appears to be an effective means to modulating the competition of energy and charge transfer. Our results are consistent with the experimental observation⁷⁴ that the electric field pointing from WS_2 to $MoSe_2$ can enhance energy transfer in $WS_2/MoSe_2$ heterostructure.

Lastly, we examine how interlayer distance may affect charge and energy transfer in vdW heterostructures^{37,38}. Specifically, we determine the energies of low-lying excitons in $WS_2/MoSe_2$ heterostructure with enlarged interlayer distances d . Note that $d = 25.3 \text{ \AA}$ is comparable to the experimental interlayer distance (6 nm) in $WS_2/hBN/MoSe_2$ heterostructure³⁷. As shown in Table 1, the energies of the interlayer excitons (\tilde{S}_2, \tilde{S}_3) increase drastically, exceeding the energy of S_0 , due to the change in the hole energy. As alluded to earlier, the hybridized valence band shown in Supplementary Fig. 3 drops its energy as the interlayer distance d is increased. In contrast, the energies of the intralayer excitons (S_{Mo} and S_0) are barely affected since their electrons and holes are at the same layer. Hence, as the interlayer distance d increases,

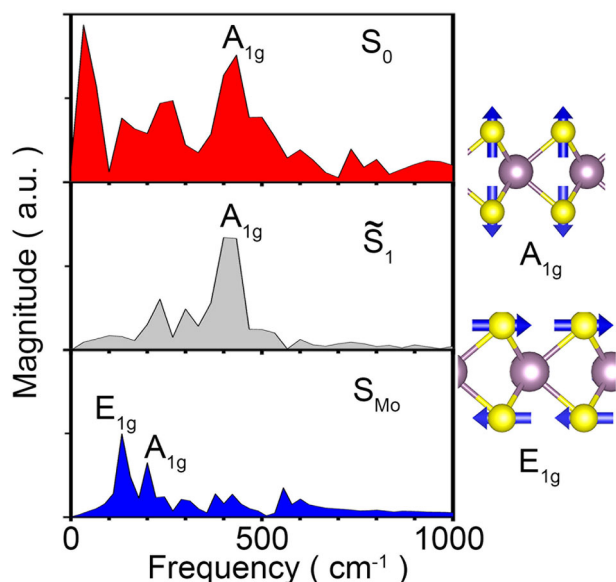


Fig. 4 Fourier transform of time-dependent energy variation of S_0 , S_1 , and S_{Mo} . The schematic illustration of A_{1g} and E_{1g} modes in WS_2 (or $MoSe_2$) monolayer is also shown. The purple and yellow spheres represent W (or Mo) and S (or Se) atoms, respectively.

charge transfer (via the interlayer excitons) is suppressed and as a result, energy transfer is expected to increase. For the same reason, Dexter mechanism involving electron-hole transfer is switched off and Förster mechanism becomes active for energy transfer at large distances ($>1 \text{ nm}$)^{40,75}. In other words, both the energy transfer efficiency and mechanism are dependent on interlayer distance. Once again, our results agree with the experimental observation that the PL intensity of $MoSe_2$ A exciton is increased in $WS_2/hBN/MoSe_2$ compared to $WS_2/MoSe_2$ at the same excitation energy of 2.0 eV ³⁷.

DISCUSSION

Before closing, we discuss two points relevant to the experiments. In the work of Kozawa et al.³⁷, $MoSe_2$ and WS_2 monolayers were randomly stacked and as a result no moiré excitons were observed. Accordingly, we do not consider moiré excitons in the present work. In addition, the screening effect due to the quartz substrate is not considered in present study. Previous first-principles calculations⁷⁶ suggested that the effect of substrate screening is less important in TMDs. In particular, the reduction in exciton binding energy due to the substrate screening is roughly offset by the renormalization of the quasiparticle band gap, thus the optical gap (or the exciton energy) remains unchanged. In other words, the energy differences between the excitons are not expected to change substantially and the same for their dynamics. We also believe that the energy transfer mechanisms remain effective, although their relative contributions may be altered somewhat by the substrate screening.

In summary, we provide a first-principles and comprehensive description of energy and charge transfer in type-II $WS_2/MoSe_2$ heterostructure. Focused on the dynamics of low-energy interlayer and intralayer excitons, we reveal that the charge and energy transfer proceeds by an ultrafast decay (10–50 fs) of the initial excitation to intermediate hot excitons, followed by a slower relaxation (100–200 fs) to the lowest-energy excitons. Under

Table 1. The energies of different excitons.

d (Å)	S_0	\tilde{S}_3	\tilde{S}_2	S_{Mo}	\tilde{S}_1
3.3 Å	2.01	1.80	1.75	1.65	1.64
8.3 Å	2.01	>2.5	>2.5	1.65	1.67
25.3 Å	2.01	>2.5	>2.5	1.64	1.79
$E = 0.1 \text{ V/Å}$	1.99	1.75	1.73	1.64	1.75
$d = 3.3 \text{ Å}$					

The energies (eV) of the excitons with different interlayer distances d and with the applied electric field (last row).

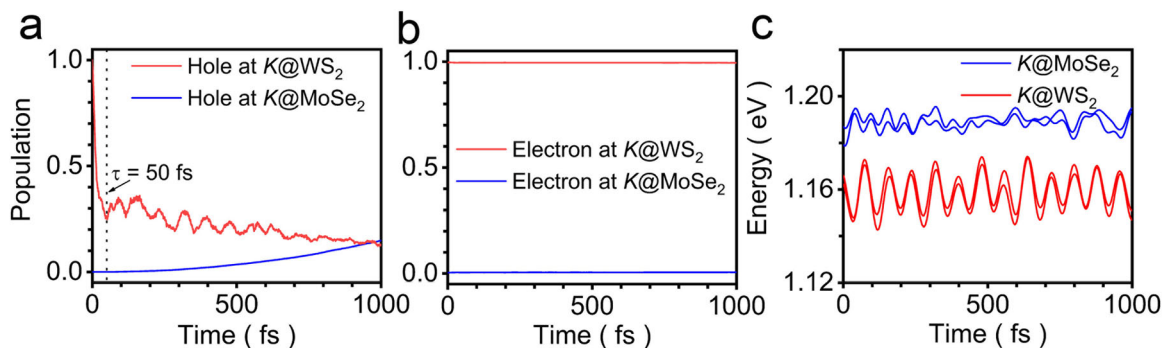


Fig. 5 Results from single-particle NAMD simulations. Time-dependent population of the “excited” hole (a) and electron (b) at 50 K from the single-particle NAMD simulations without considering the excitonic effect. c Time evolution of the KS energy levels for the “excited” electron at K-valley of WS_2 (Red) and $MoSe_2$ (blue) layer from the BOMD simulation at 50 K.

equilibrium conditions, charge transfer is ~ 2 times more efficient than energy transfer. However, the energy transfer efficiency can be doubled by applying an electric field of 0.1 V/\AA pointing from WS_2 to MoSe_2 . One can further boost the energy transfer efficiency by increasing the interlayer distance. The prevalence of low-energy dark excitons precludes Förster mechanism from playing an important role in energy transfer and Dexter mechanism is found to be responsible for energy transfer in the equilibrium heterostructure. However, when the interlayer distance is increased, the direct exchange of the electron and hole across the interface is suppressed, hence the Dexter mechanism is no longer effective, and Förster energy transfer mechanism takes over. While the dynamics of energy and charge transfer may be enhanced by coupling to different phonon modes, they exhibit a weak temperature dependence. Instead, the ultrafast and efficient energy and charge transfer in $\text{WS}_2/\text{MoSe}_2$ heterostructure is driven primarily by the excitonic effect. Complementary to experiments, our first-principles framework represents a powerful tool in rational design of novel vdW heterostructures for optoelectronic and photovoltaic applications.

METHODS

Computational models and details

As shown in Fig. 1a, the $\text{MoSe}_2/\text{WS}_2$ heterobilayer is modeled by a hexagonal unit cell (blue dashed box) containing 75 atoms with 16.1° misorientation and a negligible (0.06%) lattice mismatch between the two constituent monolayers. In order to capture the thermodynamics accurately in the ab initio BOMD simulations, we also adopted an orthogonal supercell (red dashed box) containing 450 atoms in the ab initio MD and the corresponding LR-TDDFT calculations. A vacuum slab of 15 \AA is included in the supercell to remove spurious interactions between the periodic images. After an initial structural relaxation, ab initio BOMD simulations are performed to heat up the heterobilayer to a given temperature following the velocity rescaling protocol. The temperature is then kept for 2 ps to reach the thermal equilibrium, and finally a microcanonical BOMD production run is carried out for 2 ps with a timestep of 1 fs. The SOC is included in the calculation of the exciton energies and wavefunctions via the first-order perturbation theory⁷⁷. The time-dependent population of each exciton is determined by averaging 2×10^4 NAMD trajectories. The oscillator strengths of the excitons are calculated by a recently developed LR-TDDFT method⁷⁸ based on a stochastic formulation of range-separated hybrid functionals. The range-separation parameters used in the stochastic LR-TDDFT calculations are the same as those in the (TD)DFT-OT-SRSH method. The structural relaxation and BOMD simulations are carried out with the Vienna ab initio Simulation Package (VASP)⁷⁹, using the projector-augmented-wave potentials⁸⁰ with an energy cutoff of 400 eV and the generalized gradient approximation in the Perdew-Burke-Ernzerhof (PBE)⁸¹ form for the XC functional. The semiempirical DFT-D2 method⁸² is adopted to account for the vdW interaction between the monolayers.

DATA AVAILABILITY

The data that support this work are available in the article and Supplementary information file. Further raw data are available from the corresponding author (G.L.) upon request.

CODE AVAILABILITY

The related codes are available from the authors upon reasonable request.

Received: 13 July 2021; Accepted: 1 November 2021;

Published online: 29 November 2021

REFERENCES

- Geim, A. K. & Grigorieva, I. V. Van der Waals heterostructures. *Nature* **499**, 419–425 (2013).

- Novoselov, K. S., Mishchenko, A., Carvalho, A. & Castro Neto, A. H. 2D materials and van der Waals heterostructures. *Science* **353**, aac9439 (2016).
- Jin, C. et al. Ultrafast dynamics in van der Waals heterostructures. *Nat. Nanotechnol.* **13**, 994–1003 (2018).
- Wang, Z. et al. Evidence of high-temperature exciton condensation in two-dimensional atomic double layers. *Nature* **574**, 76–80 (2019).
- Cao, Y. et al. Unconventional superconductivity in magic-angle graphene superlattices. *Nature* **556**, 43–50 (2018).
- Cao, Y. et al. Correlated insulator behaviour at half-filling in magic-angle graphene superlattices. *Nature* **556**, 80–84 (2018).
- Zhong, D. et al. Van der Waals engineering of ferromagnetic semiconductor heterostructures for spin and valleytronics. *Sci. Adv.* **3**, e1603113 (2017).
- Koperski, M. et al. Single photon emitters in exfoliated WSe_2 structures. *Nat. Nanotechnol.* **10**, 503–506 (2015).
- Feng, J., Qian, X., Huang, C.-W. & Li, J. Strain-engineered artificial atom as a broad-spectrum solar energy funnel. *Nat. Photonics* **6**, 866–872 (2012).
- Wang, Q. H., Kalantar-Zadeh, K., Kis, A., Coleman, J. N. & Strano, M. S. Electronics and optoelectronics of two-dimensional transition metal dichalcogenides. *Nat. Nanotechnol.* **7**, 699–712 (2012).
- Xiao, D., Liu, G.-B., Feng, W., Xu, X. & Yao, W. Coupled spin and valley physics in monolayers of MoS_2 and other group-VI dichalcogenides. *Phys. Rev. Lett.* **108**, 196802 (2012).
- Xu, X., Yao, W., Xiao, D. & Heinz, T. F. Spin and pseudospins in layered transition metal dichalcogenides. *Nat. Phys.* **10**, 343–350 (2014).
- Hill, H. M. et al. Observation of excitonic Rydberg states in monolayer MoS_2 and WS_2 by photoluminescence excitation spectroscopy. *Nano Lett.* **15**, 2992–2997 (2015).
- Chernikov, A. et al. Exciton binding energy and nonhydrogenic Rydberg series in monolayer WS_2 . *Phys. Rev. Lett.* **113**, 076802 (2014).
- Shi, H., Pan, H., Zhang, Y.-W. & Yakobson, B. I. Quasiparticle band structures and optical properties of strained monolayer MoS_2 and WS_2 . *Phys. Rev. B* **87**, 155304 (2013).
- Ramasubramaniam, A. Large excitonic effects in monolayers of molybdenum and tungsten dichalcogenides. *Phys. Rev. B* **86**, 115409 (2012).
- Qiu, D. Y., da Jornada, F. H. & Louie, S. G. Optical spectrum of MoS_2 : many-body effects and diversity of exciton states. *Phys. Rev. Lett.* **111**, 216805 (2013).
- Cudazzo, P., Attaccalite, C., Tokatly, I. V. & Rubio, A. Strong charge-transfer excitonic effects and the Bose–Einstein exciton condensate in graphane. *Phys. Rev. Lett.* **104**, 226804 (2010).
- Deilmann, T. & Thygesen, K. S. Interlayer excitons with large optical amplitudes in layered van der Waals materials. *Nano Lett.* **18**, 2984–2989 (2018).
- Ye, Z. et al. Probing excitonic dark states in single-layer tungsten disulphide. *Nature* **513**, 214–218 (2014).
- Rivera, P. et al. Observation of long-lived interlayer excitons in monolayer MoSe_2 - WSe_2 heterostructures. *Nat. Commun.* **6**, 6242 (2015).
- Wang, G. et al. Colloquium: excitons in atomically thin transition metal dichalcogenides. *Rev. Mod. Phys.* **90**, 021001 (2018).
- Li, M., Chen, J.-S. & Cotlet, M. Light-induced interfacial phenomena in atomically thin 2D van der Waals material hybrids and heterojunctions. *ACS Energy Lett.* **4**, 2323–2335 (2019).
- Jailaubekov, A. E. et al. Hot charge-transfer excitons set the time limit for charge separation at donor/acceptor interfaces in organic photovoltaics. *Nat. Mater.* **12**, 66–73 (2013).
- Zhang, L., Mohamed, H. H., Dillert, R. & Bahnemann, D. Kinetics and mechanisms of charge transfer processes in photocatalytic systems: a review. *J. Photochem. Photobiol. C* **13**, 263–276 (2012).
- García de Arquer, F. P., Armin, A., Meredith, P. & Sargent, E. H. Solution-processed semiconductors for next-generation photodetectors. *Nat. Rev. Mater.* **2**, 16100 (2017).
- Achermann, M. et al. Energy-transfer pumping of semiconductor nanocrystals using an epitaxial quantum well. *Nature* **429**, 642–646 (2004).
- Peng, W. et al. Hybrid light sensor based on ultrathin Si nanomembranes sensitized with CdSe/ZnS colloidal nanocrystal quantum dots. *Nanoscale* **7**, 8524–8530 (2015).
- Braud, A. et al. Energy-transfer processes in Yb:Ti-doped KY_3F_{10} , LiYF_4 , and BaY_2F_8 single crystals for laser operation at 1.5 and 2.3 μm . *Phys. Rev. B* **61**, 5280–5292 (2000).
- Hong, X. et al. Ultrafast charge transfer in atomically thin MoS_2/WS_2 heterostructures. *Nat. Nanotechnol.* **9**, 682–686 (2014).
- Ceballos, F., Bellus, M. Z., Chiu, H.-Y. & Zhao, H. Ultrafast charge separation and indirect exciton formation in a MoS_2 - MoSe_2 van der Waals heterostructure. *ACS Nano* **8**, 12717–12724 (2014).
- Pan, S., Ceballos, F., Bellus, M. Z., Zereski, P. & Zhao, H. Ultrafast charge transfer between MoTe_2 and MoS_2 monolayers. *2D Mater.* **4**, 015033 (2016).

33. Yamaoka, T. et al. Efficient photocarrier transfer and effective photoluminescence enhancement in type I monolayer $\text{MoTe}_2/\text{WSe}_2$ heterostructure. *Adv. Funct. Mater.* **28**, 1801021 (2018).
34. Bellus, M. Z. et al. Type-I van der Waals heterostructure formed by MoS_2 and ReS_2 monolayers. *Nanoscale Horiz.* **2**, 31–36 (2017).
35. Li, M. et al. A type-I van der Waals heterobilayer of $\text{WSe}_2/\text{MoTe}_2$. *Nanotechnology* **29**, 335203 (2018).
36. Wu, L., Chen, Y., Zhou, H. & Zhu, H. Ultrafast energy transfer of both bright and dark excitons in 2D van der Waals heterostructures beyond dipolar coupling. *ACS Nano* **13**, 2341–2348 (2019).
37. Kozawa, D. et al. Evidence for fast interlayer energy transfer in $\text{MoSe}_2/\text{WS}_2$ heterostructures. *Nano Lett.* **16**, 4087–4093 (2016).
38. Xu, W. et al. Controlling photoluminescence enhancement and energy transfer in $\text{WS}_2/\text{hBN}/\text{WS}_2$ vertical stacks by precise interlayer distances. *Small* **16**, 1905985 (2020).
39. Xu, W. et al. Determining the optimized interlayer separation distance in vertical stacked 2D $\text{WS}_2/\text{hBN}/\text{MoS}_2$ heterostructures for exciton energy transfer. *Small* **14**, 1703727 (2018).
40. Förster, T. Zwischenmolekulare energiewanderung und fluoreszenz. *Ann. Phys. (Berl.)*. **437**, 55–75 (1948).
41. Dexter, D. L. A theory of sensitized luminescence in solids. *J. Chem. Phys.* **21**, 836–850 (1953).
42. Liu, J., Zhang, X. & Lu, G. Excitonic effect drives ultrafast dynamics in van der Waals heterostructures. *Nano Lett.* **20**, 4631–4637 (2020).
43. Hedin, L. New method for calculating the one-particle Green's function with application to the electron-gas problem. *Phys. Rev.* **139**, A796 (1965).
44. Hybertsen, M. S. & Louie, S. G. Electron correlation in semiconductors and insulators: band gaps and quasiparticle energies. *Phys. Rev. B* **34**, 5390 (1986).
45. Rohlfing, M. & Louie, S. G. Electron-hole excitations in semiconductors and insulators. *Phys. Rev. Lett.* **81**, 2312 (1998).
46. Gross, E. K. U. & Kohn, W. Local density-functional theory of frequency-dependent linear response. *Phys. Rev. Lett.* **55**, 2850 (1985).
47. Marques, M. A., Maitra, N. T., Nogueira, F. M., Gross, E. K. & Rubio, A. *Fundamentals of Time-Dependent Density Functional Theory* Vol. 837 (Springer Science & Business Media, 2012).
48. Refaely-Abramson, S., Jain, M., Sharifzadeh, S., Neaton, J. B. & Kronik, L. Solid-state optical absorption from optimally tuned time-dependent range-separated hybrid density functional theory. *Phys. Rev. B* **92**, 081204(R) (2015).
49. Refaely-Abramson, S. et al. Gap renormalization of molecular crystals from density-functional theory. *Phys. Rev. B* **88**, 081204(R) (2013).
50. Refaely-Abramson, S. et al. Quasiparticle spectra from a nonempirical optimally tuned range-separated hybrid density functional. *Phys. Rev. Lett.* **109**, 226405 (2012).
51. Wing, D. et al. Comparing time-dependent density functional theory with many-body perturbation theory for semiconductors: Screened range-separated hybrids and the GW plus Bethe-Salpeter approach. *Phys. Rev. Mater.* **3**, 064603 (2019).
52. Zhang, X., Li, Z. & Lu, G. A non-self-consistent range-separated time-dependent density functional approach for large-scale simulations. *J. Phys. Condens. Matter* **24**, 205801 (2012).
53. Huang, L.-y., Zhang, X., Zhang, M. & Lu, G. Effect of point defects on optical properties of graphene fluoride: a first-principles study. *J. Phys. Chem. C*. **121**, 12855–12862 (2017).
54. Huang, L.-y., Zhang, X., Zhang, M. & Lu, G. Optically inactive defects in monolayer and bilayer phosphorene: a first-principles study. *Phys. Rev. Mater.* **2**, 054003 (2018).
55. Gao, Y., Zhang, M., Zhang, X. & Lu, G. Decreasing exciton binding energy in two-dimensional halide perovskites by lead vacancies. *J. Phys. Chem. Lett.* **10**, 3820–3827 (2019).
56. Nan, G., Zhang, X. & Lu, G. Self-healing of photocurrent degradation in perovskite solar cells: the role of defect-trapped excitons. *J. Phys. Chem. Lett.* **10**, 7774–7780 (2019).
57. Zhang, L., Zhang, X. & Lu, G. Band alignment in two-dimensional halide perovskite heterostructures: type I or type II? *J. Phys. Chem. Lett.* **11**, 2910–2916 (2020).
58. Zhang, L., Zhang, X. & Lu, G. Intramolecular band alignment and spin-orbit coupling in two-dimensional halide perovskites. *J. Phys. Chem. Lett.* **11**, 6982–6989 (2020).
59. Gao, Y., Liu, J., Zhang, X. & Lu, G. Unraveling structural and optical properties of two-dimensional $\text{Mo}_x\text{W}_{1-x}\text{S}_2$ alloys. *J. Phys. Chem. C*. **125**, 774–781 (2021).
60. Guo, H., Zhang, X. & Lu, G. Shedding light on moiré excitons: a first-principles perspective. *Sci. Adv.* **6**, eabc5638 (2020).
61. Zhang, X., Li, Z. & Lu, G. First-principles simulations of exciton diffusion in organic semiconductors. *Phys. Rev. B* **84**, 235208 (2011).
62. Tully, J. C. Molecular dynamics with electronic transitions. *J. Chem. Phys.* **93**, 1061–1071 (1990).
63. Duncan, W. R., Craig, C. F. & Prezhdo, O. V. Time-domain ab initio study of charge relaxation and recombination in dye-sensitized TiO_2 . *J. Am. Chem. Soc.* **129**, 8528–8543 (2007).
64. Fischer, S. A., Habenicht, B. F., Madrid, A. B., Duncan, W. R. & Prezhdo, O. V. Regarding the validity of the time-dependent Kohn-Sham approach for electron-nuclear dynamics via trajectory surface hopping. *J. Chem. Phys.* **134**, 024102 (2011).
65. Wu, G., Li, Z., Zhang, X. & Lu, G. Charge separation and exciton dynamics at polymer/ ZnO interface from first-principles simulations. *J. Phys. Chem. Lett.* **5**, 2649–2656 (2014).
66. Li, Z., Zhang, X. & Lu, G. Exciton diffusion in disordered small molecules for organic photovoltaics: insights from first-principles simulations. *J. Phys. Condens. Matter* **26**, 185006 (2014).
67. Liu, J. et al. Charge separation boosts exciton diffusion in fused ring electron acceptors. *J. Mater. Chem. A* **8**, 23304–23312 (2020).
68. Heyd, J., Scuseria, G. E. & Ernzerhof, M. Hybrid functionals based on a screened Coulomb potential. *J. Chem. Phys.* **118**, 8207–8215 (2003).
69. Ceballos, F., Bellus, M. Z., Chiu, H.-Y. & Zhao, H. Probing charge transfer excitons in a $\text{MoSe}_2/\text{WS}_2$ van der Waals heterostructure. *Nanoscale* **7**, 17523–17528 (2015).
70. Zhang, L. et al. Twist-angle dependence of moiré excitons in $\text{WS}_2/\text{MoSe}_2$ heterobilayers. *Nat. Commun.* **11**, 5888 (2020).
71. Chen, H. et al. Ultrafast formation of interlayer hot excitons in atomically thin MoS_2/WS_2 heterostructures. *Nat. Commun.* **7**, 1–8 (2016).
72. Zhu, H. et al. Interfacial charge transfer circumventing momentum mismatch at two-dimensional van der Waals heterojunctions. *Nano Lett.* **17**, 3591–3598 (2017).
73. Li, Y. et al. Ultrafast interlayer electron transfer in incommensurate transition metal dichalcogenide homobilayers. *Nano Lett.* **17**, 6661–6666 (2017).
74. Meng, Y. et al. Electrical switching between exciton dissociation to exciton funneling in $\text{MoSe}_2/\text{WS}_2$ heterostructure. *Nat. Commun.* **11**, 2640 (2020).
75. May, V. & Kühn, O. *Charge and Energy Transfer Dynamics in Molecular Systems* (John Wiley & Sons, 2008).
76. Qiu, D. Y., da Jornada, F. H. & Louie, S. G. Environmental screening effects in 2D materials: renormalization of the bandgap, electronic structure, and optical spectra of few-layer black phosphorus. *Nano Lett.* **17**, 4706–4712 (2017).
77. Qiu, D. Y., da Jornada, F. H. & Louie, S. G. Screening and many-body effects in two-dimensional crystals: monolayer MoS_2 . *Phys. Rev. B* **93**, 235435 (2016).
78. Zhang, X., Lu, G., Baer, R., Rabani, E. & Neuhauser, D. Linear-response time-dependent density functional theory with stochastic range-separated hybrids. *J. Chem. Theory Comput.* **16**, 1064–1072 (2020).
79. Kresse, G. & Furthmüller, J. Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set. *Phys. Rev. B* **54**, 11169 (1996).
80. Blöchl, P. E. Projector augmented-wave method. *Phys. Rev. B* **50**, 17953 (1994).
81. Perdew, J. P., Burke, K. & Ernzerhof, M. Generalized gradient approximation made simple. *Phys. Rev. Lett.* **77**, 3865 (1996).
82. Grimme, S. Semiempirical GGA-type density functional constructed with a long-range dispersion correction. *J. Comput. Chem.* **27**, 1787–1799 (2006).

ACKNOWLEDGEMENTS

We acknowledge the funding support from the US National Science Foundation (DMR1828019) and the US Army Research Office (W911NF-20-10305).

AUTHOR CONTRIBUTIONS

G.L. designed the project; J.L. carried out the computation and data analysis with the assistance of Z.L. and X.Z.; G.L. supervised the research and wrote the paper with J.L. All authors discussed the results.

COMPETING INTERESTS

The authors declare no competing interests.

ADDITIONAL INFORMATION

Supplementary information The online version contains supplementary material available at <https://doi.org/10.1038/s41524-021-00663-w>.

Correspondence and requests for materials should be addressed to Gang Lu.

Reprints and permission information is available at <http://www.nature.com/reprints>

Publisher's note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the

article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit <http://creativecommons.org/licenses/by/4.0/>.

© The Author(s) 2021